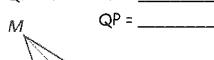
Medians and Altitudes of Triangles

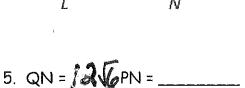
1. Name the four types of **Points of Concurrency**. Which lines intersect to form each of the points?

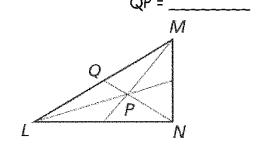
Point of Concurrency	Special Segment
1.	
2.	
3.	
4.	

2. The length of a segment from a vertex to the **Centroid** is ______the length of the median from that vertex

For #3 - 6, point P is the **Centroid** of Δ LMN.



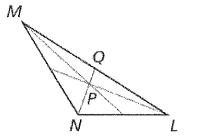




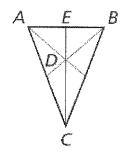
4.
$$QN = -PN = \frac{9x + 8}{2x}$$

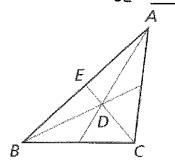
$$QP = \frac{3x}{2}$$

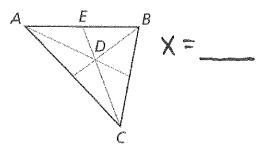
M



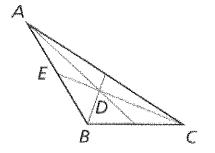
For #7 - 10, point D is the **Centroid** of $\triangle ABC$.



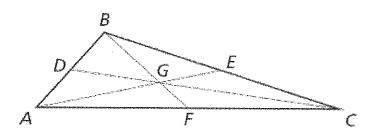




10. DE =
$$15x$$
 CD = $19x + 220$ CE = _____



For #11 - 14, point G is the **Centroid** of $\triangle ABC$. BG = 6, AF = 12, DC = 15, EG = 4, and BE = 8. Find the length of each segment. Label the triangle. Show all work.



15. Find the coordinates of the Centroid of the triangle with the given vertices

$$S(5, 5)$$
 $T(11, -3)$ $U(-1, 1)$

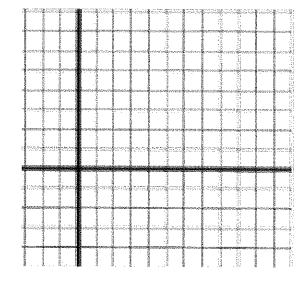
$$U(-1, 1)$$

MidpointsT:

Midpoint TU:

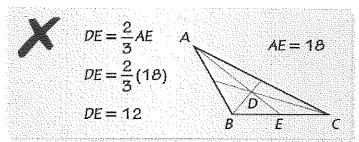
Midpointsu:

Coordinates of the Centroid:

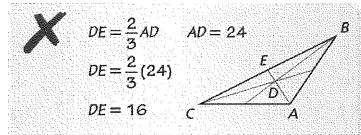


For #16 - 17, describe and correct the error in finding DE. Point D is the Centroid of $\triangle ABC$

16.

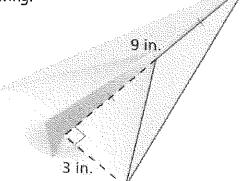


*1*7.



18. Find the area of the triangular part of the paper airplane wing.

Area = _____

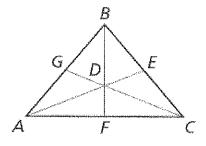


Which special segment of the triangle did you use?

For #19 - 22, point D is the Centroid of $\triangle ABC$. Use the given information to find the value of x.

19.
$$BD = 4x + 5$$

$$BF = 9x$$



20.
$$GD = 2x - 8$$
 $GC = 3x + 3$ $x =$

$$GC = 3x + 3$$

21.
$$AD = 5x$$

$$DE = 3x - 2$$

22. DF =
$$4x - 1$$
 BD = $6x + 4$ $x = ______$

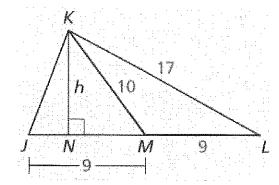
$$BD = 6x + 4$$

23. In what type of triangles can a vertex be one of the points of concurrency of the triangle? Explain your reasoning.

For #24 - 28, use the figure.

24. What type of segment is \overline{KM} ?





26. What type of segment is \overline{KN} ?

27. Which point of concurrency lies on \overline{KN} ?

28. Compare the areas of Δ JKM and Δ KLM.

Area of ΔJKM = _____

Area of Δ KLM = _____

Do you think the areas of the triangles formed by the median of any triangle will always compare this way? Explain your reasoning.

29. Your friend claims that it is possible for the Circumcenter, Incenter, Centroid, and Orthocenter to all be the same point. Do you agree? Explain your reasoning.

For #30 - 35, complete the statement with always, sometimes, or never. Explain your reasoning.

- 30. The Centroid is ______ on the triangle.
- 31. The Orthocenter is _____ outside the triangle.
- 32. A Median is ______ the same line segment as a perpendicular bisector.
- 33. An Altitude is ______ the same line segment as an angle bisector.
- 34. The Centroid and Orthocenter are ______ the same point.
- 35. The Centroid is ______ formed by the intersection of the three medians.